# Dvoretsky's <br> <br> Endgame Manual 

 <br> <br> Endgame Manual}

by Mark Dvoretsky

Fifth Edition Revised by Karsten Müller Foreword by Vladimir Kramnik


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Russell Enterprises, Inc. Milford, CT USA

## Dvoretsky's Endgame Manual

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## Table of Contents

From the Author, First Edition ..... 8
Introduction to the Fifth Edition ..... 11
Foreword by Vladimir Kramnik ..... 12
Other Signs, Symbols, and Abbreviations ..... 13
Chapter 1 Pawn Endgames
Key Squares ..... 14
Corresponding Squares ..... 15
Opposition ..... 15
Mined Squares ..... 19
Triangulation ..... 21
Other Cases of Correspondence ..... 23
King vs. Passed Pawns ..... 25
The Rule of the Square ..... 25
Réti's Idea ..... 26
The Floating Square ..... 28
Three Connected Pawns ..... 30
Queen vs. Pawns ..... 31
Knight or Center Pawn ..... 31
Rook or Bishop Pawn ..... 31
Pawn Races ..... 33
The Active King ..... 36
Zugzwang ..... 37
Widening the Beachhead ..... 37
The King Routes ..... 39
Zigzag ..... 39
The Pendulum ..... 40
Shouldering ..... 41
Breakthrough ..... 42
The Outside Passed Pawn ..... 46
Two Rook Pawns with an Extra Pawn on the Opposite Wing ..... 48
The Protected Passed Pawn ..... 53
Two Pawns to One ..... 53
Multi-Pawn Endgames ..... 54
Undermining ..... 56
Two Connected Passed Pawns ..... 57
Stalemate ..... 59
The Stalemate Refuge ..... 59
"Semi-Stalemate" ..... 60
Reserve Tempi ..... 62
Exploiting Reserve Tempi ..... 62
Steinitz's Rule ..... 64
The g- and h-Pawns vs. the h-Pawn ..... 65
The f- and h-Pawns vs. the h-Pawn ..... 66
Both Sides have Reserve Tempi ..... 69
Chapter 2 Knight versus Pawns
King in the Corner ..... 72
Mate ..... 72
Drawn Positions ..... 72
Knight vs. Rook Pawn ..... 74
The Knight Defends the Pawn ..... 76
Chapter 3 Knight Endgames
The Deflecting Knight Sacrifice ..... 80
Botvinnik's Formula ..... 81
Pawns on the Same Side ..... 85
Chapter 4 Bishop versus Pawns
The Elementary Fortresses ..... 92
Bishop and Rook Pawn ..... 92
Pawns at h6 and h7 ..... 96
Pawns at g6 and g7 ..... 97
Bishop at h7 and Pawn at g6 ..... 97
Bishop vs. Disconnected Pawns ..... 99
Bishop vs. Connected Pawns ..... 100
Chapter 5 Opposite-Color Bishops
The Most Important Rules ..... 103
Bishop and Two Connected Pawns vs. Bishop ..... 104
Separated Passed Pawns ..... 107
The King Blockades the Passed Pawn ..... 111
The Bishop Restrains the Passed Pawn ..... 115
Chapter 6 Bishops of the Same Color
Minimal Material ..... 119
Bishop and Pawn vs. Bishop ..... 119
Transposition to Positions with One Pawn ..... 120
Interference ..... 122
The Bad Bishop ..... 123
Fixing Pawns ..... 123
Zugzwang ..... 124
Pawns Which Do Not "Play by the Rules" ..... 125
Barrier ..... 130
Chapter 7 Bishop versus Knight
Bishop and Pawn vs. Knight ..... 132
Knight and Pawn vs. Bishop ..... 134
The Bishop is Superior to the Knight ..... 136
Cutting the Knight Off ..... 136
Fixing the Pawns ..... 137
The Passed Pawn ..... 138
An Open Position, A More Active King ..... 140
Defensive Methods with a Knight against a Bishop ..... 143
The Knight is Superior to the Bishop ..... 145
Domination and Knight Forks ..... 145
Fixing the Pawns ..... 146
Closed Position, Bad Bishop ..... 147
Chapter 8 Rook versus Pawns
Rook vs. One Pawn ..... 151
"Moving Downstairs" ..... 151
Cutting the King Off ..... 151
Pawn Promotion to a Knight ..... 151
Stalemate ..... 152
An Intermediate Check for a Gain of Tempo ..... 152
Shouldering ..... 153
Outflanking ..... 153
Rook vs. Connected Pawns ..... 155
Rook vs. Separated Pawns ..... 158
Chapter 9 Rook Endgames
Rook and Pawn vs. Rook ..... 160
The Pawn on the Seventh Rank ..... 160
The Pawn on the Sixth Rank ..... 161
The Pawn on the Fifth Rank ..... 165
The Umbrella ..... 167
The Pawn Has Not Crossed the Mid-line ..... 168
A Rook and Rook Pawn vs. a Rook ..... 171
The King is in Front of Its Own Pawn ..... 171
The Rook is in Front of the Pawn and the Pawn Is on the Seventh Rank ..... 172
The Rook is in Front of the Pawn and the
Pawn Is on the Sixth Rank ..... 173
a- and h-Pawns ..... 175
A Rook and Two Pawns vs. a Rook ..... 176
Doubled Pawns ..... 176
Connected Pawns ..... 177
f- and h-Pawns ..... 179
Other Pairs of Disconnected Pawns ..... 182
A Far Advanced Passed Pawn ..... 184
Transition to a Rook vs. Pawns Endgame ..... 184
Lasker's Idea ..... 186
A Rook and Two Pawns vs. a Rook and Pawn ..... 187
All Pawns are on the Same Wing ..... 187
Pawns on Opposite Wings ..... 191
Disconnected Pawns, One of them is Passed ..... 195
Four Pawns vs. Three on the Same Wing ..... 199
Balance on One Wing and an Extra Pawn on Another ..... 205
The Rook Behind Its Own Pawn ..... 205
The Rook in Front of the Pawn, with the
Pawn on the Seventh Rank ..... 208
The Rook in Front of the Pawn, with the Pawn on the Sixth Rank ..... 215
A Knight Pawn ..... 229
When the Attacker Achieves g3-g4 ..... 235
The Rook at the Side of the Pawn ..... 238
Common Observations about Endgames with Many Pawns ..... 242
The Rook's Activity ..... 242
The King's Activity ..... 246
The King on the Edge ..... 248
Cutting the King Off ..... 250
Akiba Rubinstein's Masterpiece ..... 251
Chapter 10 Rook versus Knight
The Lone Knight ..... 255
Rook and Pawn vs. Knight and Pawn ..... 256
Multi-Pawn Endgames ..... 261
Pawns on One Side of the Board ..... 261
Pawns on Both Sides ..... 264
When the Knight is Stronger than the Rook ..... 265
Chapter 11 Rook versus Bishop
The Lone Bishop ..... 267
The Dangerous Corner ..... 267
The Safe Corner ..... 268
A Bishop Pawn ..... 270
Rook and Pawn vs. Bishop and Pawn ..... 271
The Pawns are on the Same File or on Adjacent Files ..... 271
Rook Pawns ..... 275
Two Pawns vs. Two on the Same Wing ..... 278
Three Pawns vs. Three on the Same Wing ..... 282
Chapter 12 Queen Endgames
Queen and Pawn vs. Queen ..... 284
Winning Tactical Tricks ..... 287
Defensive Tactics ..... 288
Pawns on the Same Wing ..... 290
A Passed Pawn ..... 292
An Active Queen ..... 295
Chapter 13 Queen versus Rook
A Solitary Rook ..... 297
Queen vs. Rook and Pawn ..... 299
The Rook behind the Pawn ..... 299
The Pawn on the Seventh Rank ..... 300
The Pawn on the Sixth Rank ..... 301
A Knight Pawn on the Fifth or Sixth Rank ..... 304
Queen and Pawn vs. Rook and Pawn ..... 305
Passed Pawns ..... 305
Pawns on Adjacent Files ..... 307
A Fortress with Multiple Pawns ..... 308
Chapter 14 Other Material Relations
Two Extra Pieces ..... 313
Checkmating with Bishop and Knight ..... 313
Checkmating with Two Knights ..... 314
Rook and Knight vs. Rook ..... 314
Rook and Bishop vs. Rook ..... 316
Without Pawns ..... 316
With Pawns ..... 319
An Extra Bishop or Knight with Queens or Minor Pieces ..... 320
Rook vs. Two Minor Pieces ..... 321
Queen vs. Various Pieces ..... 325
Queen vs. Two Rooks ..... 328
Chapter 15 General Endgame Ideas
King's Activity ..... 331
Pawn Power ..... 337
Zugzwang ..... 342
Fortresses ..... 345
A Fortified Camp ..... 345
A Pawn Barrier ..... 346
An Imprisoned King ..... 348
An Imprisoned Piece ..... 350
Binding ..... 351
Stalemate ..... 352
Checkmate ..... 356
Domination ..... 359
Chapter 16 Solutions ..... 362
Bibliography ..... 422
Indexes
Index of Players ..... 425
Index of Composers and Analysts ..... 434
Index of Strategic and Tactical Techniques ..... 437

## Foreword

There are many chess endgame books, and some of them are very instructive and undoubtedly are worth careful study. But in my view, Dvoretsky's Endgame Manual can be called the Bible among them because the material in it is very well structured and explained.

There are many existing theoretical endgames and it is impossible to remember them all. It is therefore necessary to select those which have a "basic structural value." I think Dvoretsky succeeded in doing this very well, making outstanding and painstaking efforts to select the "endgame knowledge base" for a chess player. The book contains all that you NEED to know and sets aside everything superfluous, or more precisely, what is not so necessary to remember.

Although of course I had fully mastered this material when the book first came out, I always had it close at hand. Before my world championship matches and candidates' tournaments, I always refreshed and reinforced these endings in my memory by glancing through this book.

Indeed, modern chess has changed a lot, and very often you have to make critical decisions with little time on the clock. A player is often faced with calculating in the seventh hour of play, trying to find the best move, for which there is often simply neither time nor energy. To handle a situation like that, it is crucial to have markers - beacons in this vast ocean of possibilities in the endgame - to know well which endings are winning and which are not, and to have at least a rough idea of how to play them.

While it is impossible to remember everything, if a chessplayer has at his command the assessment and the core criteria of play in theoretical endings, the benefits will be obvious.

Of course, it does not often happen that a precise position from the book appears on the board. But your endgame technique is certain to improve, as well as your defensive abilities. The fact is, if you know which theoretical endings you should enter and which you should not, depending on the result you are trying to achieve, this is a tremendous help in making the correct decisions in many other endgames not covered here.

I think that all chessplayers should express their gratitude to Mark Dvoretsky for undertaking such work, synthesizing in a practical format and in a condensed and well-explained form, the most important endgame knowledge which every chessplayer must possess.

Naturally, in today's world, everyone has gotten used to working with computers, and you can pull up a tablebase and see how a theoretical endgame is evaluated, what correct moves should be made. But it is impossible to attain real endgame mastery by just working with a computer. An explanation of why an endgame is winning, and how to win (or save) it from a human point of view, described in words and in language that a person understands (as opposed to computer variations), is needed.

In short, I consider Dvoretsky's Endgame Manual an absolute must for every chess professional, and no less important even for a club player. Learn the endgame principles in this book well, refresh them in your memory from time to time, and your rating and your tournament performances will surely improve.

I often get questions from both chess amateurs and professionals about which books to study to improve their play. The list is short, but have no doubt - I always recommend this book for everyone.

I consider it to be one of the very best chess books published in recent times and I am very pleased with the new enhanced edition that has come out.

## Chapter 6

## Bishops of the Same Color

## Minimal Material

## Bishop and Pawn vs. Bishop

These endgames were first subjected to thorough analysis in the mid-19th century by the Italian player Centurini. Later, significant additions to the theory were made by GM Averbakh.


White to move wins, by driving off the enemy bishop from one diagonal, and then interfering along the other diagonal.
 B6 6 +

Can this plan be prevented? Yes, it can - provided Black's king can get to c5, preventing White's bishop from interfering along the diagonal. Black to move draws:

 blat = Thus, if the weaker side's king cannot get in front of the pawn, then the basic defensive principle becomes: king behind the king!

The short diagonal: even with the "right" king position, the draw is impossible if one of the diagonals along which the bishop will restrain the pawn proves too short.


All the squares on the c8-a6 diagonal, except c8, are under the control of White pieces - that is why we get zugzwang. Now, if we were to move the entire position down one rank, the bishop would get another free square, and White could no longer win.

The following position of reciprocal zugzwang has some practical significance.


White to move only draws. 1 d5 ec8 (or





But what is Black to do if it is his move? Any bishop retreat along the h1-a8 diagonal is refuted by 2 dis; therefore, he must play 1... a6. By the way

## Dvoretsky＇s Endgame Manual

（here＇s a tragicomedy！），in this won position， Botvinnik accepted a draw against Model in the 1931 Leningrad Championship．

The path to victory is not complicated： $\mathbf{2}$ de6！
皿a6－b7＋－

## Transpositions to Positions with One Pawn

## Charushin－Rosenholz

cr 1986


A typical situation：White can take the g4－pawn only at the cost of his a6－pawn．The question is whether the enemy king can get back in time．

## 1 角f4！©

Excellently played！White improves his own king＇s position（now it no longer stands in the path of its pawn）while simultaneously using zugzwang to force the enemy king further away from the
 the 464 g 4 te leads only to a draw．



No better is 3．．．c8 4 e4 rib6 5 县5．
4 g 4 that 5 g 5 that 6 g 6 the6
Nothing is changed by 6．．．


Black resigned，in view of 8．．．f7 9 the fot 10 bh7 gig 11 th8 th6 12 昷 4 ，followed by h7－g8（the h7－g8 diagonal，where the black bish－ op must move，is too short）．

## Capablanca－Janowsky

New York 1916


White has nothing to play for，other than to pick up the b－pawn in exchange for his g6－pawn． Unfortunately，this plan would not be enough to win．

 shows that 4 ．．．f2 also draws，but that 4 ．．．h4 4 ？



## 1 ge4

Capablanca is in no hurry to force matters－he maneuvers，hoping for a mistake by his opponent．

## 1．．．b4

 Ne7 is not bad）；but，on the other hand，it does not spoil anything．



And here is the mistake！Now White captures the b4－pawn，with a tempo ahead of the other variations．First Black had to lure the king away from the queenside： $5 \ldots$ ．．．$g 7$ ！ 6 ght and now he can


## 6 tod


县e5 $\triangle$ 昷 $77+$

## 

White errs in return－although it is not at all obvious．The win was 9 d2！－a variation we shall examine later．

## 



In this position, Janowsky resigned. And wrongly so - as Averbakh has shown. Black could get a draw by employing the basic defensive plan of "king behind king."

Since White is going to put his king on c6, Black must hurry his king over to c 4 :
11...




After 17 d6 EC4, Black prevents the interference along the diagonal at c5 just in time. But the struggle is not over yet.

17 fibl


The most dangerous continuation, as pointed out by Issler. If Black now plays $17 \ldots$... B c 3 ? then 18
 Black has no time to play de 4 - White is ready to reply with either 20 (c7 or C 5 , depending on where Black's bishop retreats.

Black is saved by a tactic, which is very useful to remember: it is a typical trick in bishop endgames.
17... d2!!

On 18 b6, the pin 18... 55 saves him.

## 18 d88e3!

Now the threat of 19 b6 a5 20 b7 forces Black to retreat. That is fine - White's bishop stands worse on d8 than it did on c7, and there is no longer any danger in 19 ( $7(\triangle 20$ ( 4 ) 19... 0 b6! 20 tc6 ta5! (White no longer has 21 (c7) 21 d6 \% ty

White has just one final trap:
县d6 \%

Once again, the same technique of "king behind king": the black king heads for a4. He would lose
 $\triangle$ a5+- And 22...b4? 23 b6 24 昷 $\mathrm{B} 5+$ and $25 \mathrm{~b} 6+-$ is wrong too.

All that is left for us to see is what would have happened, had Capablanca played more precisely on his ninth move.


Now we are looking at the position from the next-to-last diagram, but with the bishop on d2 (instead of c3). Here Black's king is unable to get behind White's.

 b6+-

## Interference

We know that interference is the primary in－ strument by which the stronger side secures（or attempts to secure）the queening of its pawn．In all the examples we have looked at thus far，the bishop has done this work．But sometimes（although cer－ tainly not nearly as often），interference is carried out with the aid of the pawns．For instance，there is the following spectacular study．

## P．Heuäcker 1930



1 a7！（ 1 h 7 ？e $4=$ ）1．．． $\mathbf{1} 2$ 曷b1 $\mathbf{d} 3$
莫d3 置b2 6 筸e4＋

## Tragicomedies

We have already seen the tragicomedies that occurred in the games Botvinnik－Model and Capablanca－Janowsky．I will add one more example．

> Savchenko - Krivonosov

USSR 1989

 Black won．

The same tactical idea of interference as in the Heuäcker study brought Black success here． However，this occurred only as a result of his opponent＇s gross blunder．After 3 gid d ！exe5 （3．．．a2？ 4 g7＋－） 4 ge the king is in the square of the a－pawn．

Black should have carried out his interference in a more primitive form，by preparing ．．． e ．This could have been achieved either by $1 \ldots$ ．．．d 2 der d 3 ？ the6！（but not 2．．．a2？ 3 c4＋） 3 d 4 a2 4 c4 1 e5，or
 （3．．．${ }^{\text {bid }} \mathrm{d} 5$ ？is a mistake，because of $4 \mathrm{c} 6=$ ）．

## Exercises




The Bad Bishop
A vital principle of chess strategy（which is certainly applicable to more than just the endgame） requires us not to place our pawns on the same color squares as our own bishop．

In the first place，pawns that are fixed on the same color squares as the bishop limit its mobility－ this is why such a bishop is called＂bad．＂

In the second place，a bad bishop is unable to attack the enemy pawns（which are usually placed on the opposite color squares），which dooms it to passive defense of its own pawns．

And third，since both pawns and bishop control only one color of squares，there will be＂holes＂in between those squares that the enemy pieces will occupy．

## Fixing Pawns

Averbakh－Veresov
Moscow 1947


## 1 h 4 ！

The experienced player makes such moves－ fixing the enemy pawns on the same color squares as his bishop－without thinking．

White has a great positional advantage．After the necessary preparations，he will create an outside passed pawn on the queenside，which will divert the enemy forces，allowing White to fall upon the king－ side pawns．



The bishop aims for d 7 ，where it will support the queenside pawn advance while at the same time be ready to attack the pawn at $g 6$ ．For example：
当d5 10 具e8

 13 县 6 是c6 $14 \mathrm{~g} 4+-) 11 \mathrm{hg}$ 붑 $\times \mathrm{c} 512$ 县 6 ！ d 5




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On 9．．．d3， 10 （ 66 昷f5 11 b5（11 d7＋）



10 d $\times 4$ gh 11 gh Sa4

是d7（14．．．



 18 h5 \％igh 19 （\％f6！＋－）


## 16 e8！©

We know this technique from the ending Charushin－Rosenholz（diagram 6－4）．Before taking the pawn，it is important to drive the black king back to b 6 －as far as possible from the kingside．The hasty
 ， 7 ？leads only to a draw．

16．．．
 （analysis by Averbakh）．

## Zugzwang

With a bad bishop，the weaker side＇s defensive hopes often are destroyed through zugzwang．Here is the simplest example：

Y．Averbakh 1954


The correspondence between the f3－and f7－ squares is obvious－to win，it is necessary only to give Black the move．If you like，you can also find other pairs of corresponding squares（for example， the f1－and b3－squares also correspond to f7），but there is no real need．

1 昷e2 ${ }^{\text {B }} 8$
If $1 \ldots \mathrm{~g} 6$ ，then 2 d 3 h7 3 f1！g6


20d3 D6

 1 $13+$

Now，let＇s look at a considerably more complex endgame．

Shabalov－Varavin

Moscow 1986


## 1） 1 置b6

On 1．．． C ？ 2 and Black is in zugzwang，and must put another pawn on the same color as his bishop，making his opponent＇s winning task that much simpler．For example，2．．．g5 3 皿b2 昷d6 4

 B $3 \odot$ White＇s bishop maneuvers here in roughly the same way as it did in the preceding example．

## 2 （h4！e3

The c7－square turns out to correspond，not just to the c3－square，but also to g3．2．．． c ？ ？would be
 2．．．d4？ 3 d8 decides．

## 3（g3 dit

After 3．．． 4 ？ 4 ，Black must defend the a5－pawn with his king，and allow the enemy king to enter．This does not bode well for Black： 4 ．．． B b6 5


 queens．

4 h h ！© b2
 5 Q 1 Sa3！
 g5 8 县 $2+-$

6 Sf2 De7！
Otherwise，we get the basic zugzwang position：
道d6 8 ，etc．

## 7 （g3！d6

By means of a series of accurate maneuvers， Shabalov has achieved his aim－the bishop has been deflected onto a poor diagonal．On the other hand， there was no longer any choice： $7 \ldots \mathrm{~d}$ ？ 8 （ 1 （ 7 9 县 $\mathrm{C} 3 \odot+$


## 8 h2 $\odot$ g 9 g5！

White＂breaks the rule，＂by moving a pawn onto a square the same color as his own bishop－in order to restrict the enemy bishop＇s mobility still further． There is no other way to make any progress．

## 9．．． 88

9．．．h8？ 10 g3 g7 11 县 1 is hopeless．

## 

The decisive error．After the accurate $11 \ldots \mathrm{C} 5$
 （shown by Aczel）realizing the extra pawn is evidently not possible．

## 12 S3！

Advancing the e－pawn does nothing for White： 12 e5 d2 13 e6 to d6 14 e7 to d7．So he takes the a5－pawn in exchange for the g5－pawn．
 b5＋벙d6 16 dc3！g5 17 e5＋the7
$17 \ldots$ xe5 18 是 $\times$ e5＋웁xe5 19 b6！（but not 19

 Q $\mathbf{g 5}$（22 e7 was threatened） $\mathbf{2 2} \mathbf{b 6}$ Black resigned．

## Pawns Which Do Not ＂Play by the Rules＂

In chess，there are no absolute laws．Even so important and generally useful an axiom as the unprofitability of placing one＇s pawns on the same color squares as one＇s bishop must occasionally be broken．Here are the possible reasons for doing so：
－To restrict the mobility of the enemy bishop using one＇s own pawns（as occurred in the preced－ ing example）；
－The need to undermine the enemy pawn chain；and
－The attempt to create an impregnable fortress around a＂bad bishop．＂

The first and third points are illustrated by the following case：

## Wojtkiewicz－Khalifman

Rakvere 1993


